Micro Comprehensive Exam 2020

Part A

(Please answer BOTH questions from this part.)

1. Preferences (Rubinstein, C5)

Identify a professor's lifetime with the interval [0,1]. There are K + 1 academic ranks, 0; ...; K. All professors start at rank 0 and eventually reach rank K. De ne a career as a sequence $t = (t_1; ...; t_K)$ where $t_0 = 0$ t_1 t_2 ... t_K 1 with the interpretation that t_k is the time it takes to get the k'th promotion. (Note that a professor can receive multiple promotions at the same time.) Denote by \succeq the professor's (rational) preferences on the set of all possible careers. For any > 0 and for any career t such that t_K 1 , de ne t + to be the career $(t +)_k = t_k$ + for all k (i.e. all promotions are delayed by). Following are two properties of the professor's preferences:

Monotonicity: For any two careers t and s, if $t_k = s_k$ for all k then $t \succeq s$ and if $t_k < s_k$ for all k, then $t \succeq s$.

Invariance: For every > 0 and every two careers *t* and *s* for which *t* + and *s* + are well de ned, $t \succeq s$ if and only if $t + \succeq s + \ldots$

1. Formulate the set *L* of careers in which a professor receives all *K* promotions at the same time. Shc978 --uh9,9y 17 such that

for every individual *i*, the house a(i) maximizes *i*'s preference relation \succeq_i over her budget set $fh \ge H : p(h) = p(e(i))g$:

```
p(a(i)) = p(e(i)) and a(i) \succeq_i h for all h \ge H with p(h) = p(e(i))
```

- 1. Show that every equilibrium allocation *a* is strongly Pareto e cient; that is, for any equilibrium allocation *a*, there is no allocation $b \in a$ such that $b(i) \succeq_i a(i)$ for all $i \ge N$ and $b(i) =_i a(i)$ for some $i \ge N$.
- 2. Show that if the initial distribution *e* is strongly Pareto e cient, then for every equilibrium (*p*; *a*) we have a = e.

Part B

(Please answer BOTH questions from this part.)

3. Finitely Repeated Games

Consider the following stage game played between Benoit and Krishna with common discount factor = 3=4.

	L	Μ	R
U	8;2	1;1	5;3
С	7;1	3;3	6;4
D	4;4	4;5	1;3

Suppose the game is repeated once (therefore played twice).

a) State a pure strategy subgame perfect equilibrium.

b) Is there a pure strategy subgame perfect equilibrium in which the rst period outcome does *not* correspond to a Nash equilibrium of the stage game? If so, state it. Otherwise, explain why not.

4. *VCG*

Consider the allocation of three identical and indivisible objects to three agents, $N = f_{1,2,3g}$, each of whom can consume multiple units. Agent *i* values the consumption of *k* units of the object at v_k^i . Her valuation pro le $i = (v_{1,1}^i, v_{2,2}^i, v_{3,1}^i)$ is her private information. All that is publicly known is that for each player *i*, $0 = v_{1,2}^i = v_{2,2}^i = v_{3,2}^i$. Suppose the true valuations of the three players are as follows,

The table above shows, for instance, that player 1 has valuations $v_1^1 = 5$, $v_2^1 = 10$ and $v_3^1 = 13$.

Suppose the three players report their respective valuation pro le truthfully.

a) What is the allocation of the three objects that maximizes the sum of values (utilities) across all players, for such a pro le? (Who gets what?)

b) What are the transfers according to the VCG mechanism for this valuation pro le?

(Note: You are only required to state the allocation and transfers for *this particular* valuation pro le and not for any general valuation pro le. The correct answer involves explicit numbers and not algebraic expressions.)

Now suppose instead that Players 2 and 3 collude behind Player 1's back and both lie about their valuations, while Player 1 reports truthfully.

c) Is there an untruthful valuation pro le for players 2 and 3 that make both these players strictly better o ? If yes, provide an example. If no, explain why not.